Taking into consideration the recent advances in different areas of mathematics, the board of studies in Mathematics, after discussions with experts, has revised the syllabus of M.Sc./M. A. Mathematics course.

Aims:

1. Strengthening the logical reasoning which is the main ingredient to understand mathematical concepts.
2. Create more interest in the subject and motivate students for self learning.
3. Developing the mathematical skills among the students and preparing them to take up a career in research.

Objectives:

1. To make students understand the techniques of proof in Mathematics and apply suitable techniques to tackle problems.
2. To inculcate the habit of making observations and experimentation and arrive at the final result.
3. Make students acquire the communication skill to present technical Mathematics so as to take up a career in Teaching Mathematics at various levels including schools, colleges, universities, etc.

General e-references:

1. National Programme on Technology Enhanced Learning.(Mathematics)
   http://www.nptelvideos.com/mathematics/
2. Mathematics Video Lectures
   http://freevideolectures.com/Subject/Mathematics
3. MIT Open Course Ware
   http://ocw.mit.edu/courses/audio-video-courses/

E-references pertinent to each course are given at the end of the syllabus of the course.
SCHEME OF EXAMINATION  

Semester I

<table>
<thead>
<tr>
<th>CODE</th>
<th>SUBJECT</th>
<th>L</th>
<th>T</th>
<th>C</th>
</tr>
</thead>
<tbody>
<tr>
<td>M 111</td>
<td>Field theory</td>
<td>4</td>
<td>--</td>
<td>4</td>
</tr>
<tr>
<td>M 112</td>
<td>Real Analysis-I</td>
<td>4</td>
<td>--</td>
<td>4</td>
</tr>
<tr>
<td>M 113</td>
<td>Topology-I</td>
<td>4</td>
<td>--</td>
<td>4</td>
</tr>
<tr>
<td>M 114</td>
<td>Complex Analysis-I</td>
<td>4</td>
<td>--</td>
<td>4</td>
</tr>
<tr>
<td>M 101</td>
<td>Differential Equations-I</td>
<td>4</td>
<td>--</td>
<td>4</td>
</tr>
</tbody>
</table>

Viva-Voce 4

Contact hours : 20 per week  
Valid credits : 20  
L : Lecture  
T : Tutorial  
C : Credits

* The following notation comprising of three digits is used while numbering the courses.

1. The first digit refers to the semester number i.e. 1,2,3, and 4.
2. The second digit 1 refers to a core course and the second digit 0 refers to an optional course.
3. The third digit refers to the serial number of the course.
**SCHEME OF EXAMINATION**

**M.A. /M.Sc. Mathematics**

**Semester II**

<table>
<thead>
<tr>
<th>CODE</th>
<th>SUBJECT</th>
<th>L</th>
<th>T</th>
<th>C</th>
</tr>
</thead>
<tbody>
<tr>
<td>M 211</td>
<td>Advanced Abstract Algebra</td>
<td>4</td>
<td>--</td>
<td>4</td>
</tr>
<tr>
<td>M 212</td>
<td>Real Analysis-II</td>
<td>4</td>
<td>--</td>
<td>4</td>
</tr>
<tr>
<td>M 213</td>
<td>Topology-II</td>
<td>4</td>
<td>--</td>
<td>4</td>
</tr>
<tr>
<td>M 214</td>
<td>Complex Analysis-II</td>
<td>4</td>
<td>--</td>
<td>4</td>
</tr>
<tr>
<td>M 201</td>
<td>Differential Equations-II</td>
<td>4</td>
<td>--</td>
<td>4</td>
</tr>
</tbody>
</table>

**Viva-Voce**

Contact hours : 20 per week
Valid credits : 20
L : Lecture
T : Tutorial
C : Credits

* The following notation comprising of three digits is used while numbering the courses.

1. The first digit refers to the semester number i.e. 1,2,3, and 4.
2. The second digit 1 refers to a core course and the second digit 0 refers to an optional course.
3. The third digit refers to the serial number of the course.
SCHEME OF EXAMINATION

M.A. /M.Sc. Mathematics

Semester III

<table>
<thead>
<tr>
<th>CODE</th>
<th>SUBJECT</th>
<th>L</th>
<th>T</th>
<th>C</th>
</tr>
</thead>
<tbody>
<tr>
<td>M 311</td>
<td>Integration Theory</td>
<td>4</td>
<td>-</td>
<td>4</td>
</tr>
<tr>
<td>M 312</td>
<td>Functional Analysis</td>
<td>4</td>
<td>-</td>
<td>4</td>
</tr>
<tr>
<td>M 313</td>
<td>Partial Differential Equations</td>
<td>4</td>
<td>-</td>
<td>4</td>
</tr>
<tr>
<td>M 301</td>
<td>Theory of Linear Operators-I</td>
<td>4</td>
<td>-</td>
<td>4</td>
</tr>
<tr>
<td>M 302</td>
<td>Linear Programming-I</td>
<td>4</td>
<td>-</td>
<td>4</td>
</tr>
<tr>
<td>M 305</td>
<td>Mathematical Modelling-I</td>
<td>3</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Viva-Voce</td>
<td></td>
<td></td>
<td>4</td>
</tr>
</tbody>
</table>

Contact hours : 23 per week
Valid credits : 23
L : Lecture
T : Tutorial
C : Credits

* The following notation comprising of three digits is used while numbering the courses.

1. The first digit refers to the semester number i.e. 1, 2, 3, and 4.
2. The second digit 1 refers to a core course and the second digit 0 refers to an optional course.
3. The third digit refers to the serial number of the course.
4. M305 is an elective generic course.
## SCHEME OF EXAMINATION

### M.A. /M.Sc. Mathematics

#### Semester IV

<table>
<thead>
<tr>
<th>CODE</th>
<th>SUBJECT</th>
<th>L</th>
<th>T</th>
<th>C</th>
</tr>
</thead>
<tbody>
<tr>
<td>M 411</td>
<td>Mechanics</td>
<td>4</td>
<td>-</td>
<td>4</td>
</tr>
<tr>
<td>M 401</td>
<td>Theory of Linear Operators - II</td>
<td>4</td>
<td>-</td>
<td>4</td>
</tr>
<tr>
<td>M 402</td>
<td>Linear Programming -II</td>
<td>4</td>
<td>-</td>
<td>4</td>
</tr>
<tr>
<td>M 403</td>
<td>Homotopy Theory</td>
<td>4</td>
<td>-</td>
<td>4</td>
</tr>
<tr>
<td>M 404</td>
<td>Topics In Ring Theory</td>
<td>4</td>
<td>-</td>
<td>4</td>
</tr>
<tr>
<td>M405</td>
<td>Mathematical Modelling-II</td>
<td>3</td>
<td>--</td>
<td>3</td>
</tr>
<tr>
<td></td>
<td>Viva-Voce</td>
<td></td>
<td></td>
<td>4</td>
</tr>
</tbody>
</table>

Contact hours : 23 per week  
Credits : 23  
L : Lecture  
T : Tutorial  
C : Credits

* The following notation comprising of three digits is used while numbering the courses.

1. The first digit refers to the semester number i.e. 1, 2, 3, and 4.
2. The second digit 1 refers to a core course and the second digit 0 refers to an optional course.
3. The third digit refers to the serial number of the course.
4. M405 is an elective generic course.
CORE COURSES

Semester I

M 111  Field theory
M 112  Real Analysis-I
M 113  Topology-I
M 114  Complex Analysis-I

Semester II

M 211  Advanced Abstract Algebra
M 212  Real Analysis-II
M 213  Topology-II
M 214  Complex Analysis-II

Semester III

M 311  Integration Theory
M 312  Functional Analysis
M 313  Partial Differential Equations

Semester IV

M 411  Mechanics
# ELECTIVE COURSES (Discipline Centric)

## Semester I

<table>
<thead>
<tr>
<th>CODE</th>
<th>SUBJECT</th>
</tr>
</thead>
<tbody>
<tr>
<td>M 101</td>
<td>Differential Equations-I</td>
</tr>
<tr>
<td>M 102</td>
<td>Advanced Discrete Mathematics-I</td>
</tr>
<tr>
<td>M 103</td>
<td>Differential Geometry of Manifolds-I</td>
</tr>
</tbody>
</table>

## Semester II

<table>
<thead>
<tr>
<th>CODE</th>
<th>SUBJECT</th>
</tr>
</thead>
<tbody>
<tr>
<td>M 201</td>
<td>Differential Equations-II</td>
</tr>
<tr>
<td>M 202</td>
<td>Advanced Discrete Mathematics-II</td>
</tr>
<tr>
<td>M 203</td>
<td>Differential Geometry of Manifolds-II</td>
</tr>
</tbody>
</table>

## Semester III

<table>
<thead>
<tr>
<th>CODE</th>
<th>SUBJECT</th>
</tr>
</thead>
<tbody>
<tr>
<td>M 301</td>
<td>Theory of Linear Operators-I</td>
</tr>
<tr>
<td>M 302</td>
<td>Linear Programming-I</td>
</tr>
<tr>
<td>M 303</td>
<td>Programming in C – Theory &amp; Practical</td>
</tr>
<tr>
<td>M 304</td>
<td>Mathematics of Finance &amp; Insurance-I</td>
</tr>
</tbody>
</table>

## Semester IV

<table>
<thead>
<tr>
<th>CODE</th>
<th>SUBJECT</th>
</tr>
</thead>
<tbody>
<tr>
<td>M 401</td>
<td>Theory of Linear Operators - II</td>
</tr>
<tr>
<td>M 402</td>
<td>Linear Programming-II</td>
</tr>
<tr>
<td>M 403</td>
<td>Homotopy Theory</td>
</tr>
<tr>
<td>M 404</td>
<td>Topics In Ring Theory</td>
</tr>
<tr>
<td>M 405</td>
<td>Algebraic Topology</td>
</tr>
<tr>
<td>M 406</td>
<td>Analytical Number Theory</td>
</tr>
<tr>
<td>M 407</td>
<td>Abstract Harmonic Analysis</td>
</tr>
<tr>
<td>M 408</td>
<td>Mathematics of Finance &amp; Insurance-II</td>
</tr>
</tbody>
</table>

* Those electives will be offered for which expertise is available in the department.
ELECTIVE COURSE (Generic)

M305 Mathematical Modelling-I
M405 Mathematical Modelling-II
SYLLABUS
M.A./M.Sc. MATHEMATICS

SEMESTER I
M 111 Field theory
M 112 Real Analysis-I
M 113 Topology-I
M 114 Complex Analysis-I
M 101 Differential Equations-I

SEMESTER II
M 211 Module Theory
M 212 Real Analysis-II
M 213 Topology-II
M 214 Complex Analysis-II
M 201 Differential Equations-II

SEMESTER III
M 311 Integration Theory
M 312 Functional Analysis
M 313 Partial Differential Equations
M 301 Theory of Linear Operators-I
M 302 Linear Programming-I

SEMESTER IV
M 411 Mechanics
M 401 Theory of Linear Operators - II
M 402 Linear Programming -II
M 403 Homotopy Theory
M 404 Topics in Ring Theory

Course Plan: Each course has five units and each unit shall be covered in three weeks on average.
SEMESTER - I
M 111
FIELD THEORY

Pre-requisites: Basics on rings and fields. (relevant parts of reference [1])

Unit I:
Finite & Algebraic extensions, Algebraic closure,

Unit II:
splitting fields and normal extensions, separable extensions,

Unit III:
Finite fields, Primitive elements and purely inseparable extensions.

Unit IV:
Galois extensions, examples and applications,

Unit V:
Roots of unity, Linear independence of characters, cyclic extensions, solvable & radical extensions.

Book Recommended:
1. Serge Lang : Algebra

Reference Books:

E-references:
1. Notes on Galois Theory, Sudhir R. Ghorpade
   Department of Mathematics, Indian Institute of Technology, Bombay 400 076
   http://www.math.iitb.ac.in/~srg/Lecnotes/galois.pdf

2. Galois Theory, Dr P.M.H. Wilson.
   http://www.jch.co.uk/maths/Galois.pdf
M 112
REAL ANALYSIS-I

Pre-requisites: Chapters 1 to 5 of reference [1]

Unit I:
The Riemann-Stieltjes Integral Definition and existence of the integral, properties of the integral, integration and differentiation, integration of vector-valued functions, rectifiable curves.

Unit II:
Sequences and Series of Functions Rearrangements of terms of a series, Riemann theorem, pointwise and uniform convergence, Cauchy criterion for uniform convergence, Weiestrass M-test, uniform convergence and continuity, uniform convergence and integration.

Unit III:
Uniform convergence and differentation, equicontinuous families of functions, the Stone-Weierstrass Theorem, uniform convergence and Riemann-Stieltjes integral,

Unit IV:
Abels test for uniform convergence, Dirichlet's test for uniform convergence. power series, Abel's theorem.

Unit V:
Functions of Several Variables, derivatives in an open subset of R^n, chain rule, partial derivatives, interchange of the order of differentiation, derivatives of higher orders, inverse function theorem, implicit function theorem, Jacobians, differentiation of integrals, Taylor's theorem, extremum problems with constraints, Lagrange's multiplier method.

Books Recommended:

Reference Books:
Unit I: (Pre-requisites)

Unit II:
Topological spaces. The order topology. Product topology on X x Y. Bases and subbases. Subspaces and relative topology.

Unit III:

Unit IV:
Continuous Functions and homeomorphisms. The product topology. The metric topology. The quotient topology

Unit V:

Books Recommended:
1. James R. Munkres, Topology (Second edition), Prentice-hall of India

References:

E-references:
1. Topology Course Lecture Notes Aisling McCluskey and Brian McMaster  
   http://at.yorku.ca/i/a/a/b/23.htm
2. Notes on Introductory Point-Set Topology, Allen Hatcher 
   http://www.math.cornell.edu/~hatcher/Top/TopNotes.pdf
3. Introduction to Topology, Renzo 
   http://www.math.colostate.edu/~renzo/teaching/Topology10/Notes.pdf
4. Topology Lecture Notes, Thomas Ward, UEA 
   http://www.uea.ac.uk/~h720/teaching/topology/materials/topology.pdf
M 114
COMPLEX ANALYSIS-I

Pre-requisites:
Basic Metric space theory: relevant parts of reference [1]

Unit I: Algebra of complex numbers, geometric aspects like equations to straight lines, circles, analytic functions, exponential , trigonometric, hyperbolic functions, Branches of many valued functions with special reference to arg \( z \), log \( z \), and complex exponents.

Unit II:

Unit III:
Taylor's theorem, Maximum Modulus Principle, Schwarz Lemma.

Unit IV:
Isolated singularities, Meromorphic functions, Laurent's series, Argument Principle, Rouche's theorem.

Unit V:
Residues, Cauchy's Residue theorem, evaluation of integrals, their properties and classification, definitions and examples of conformal mappings, Hadamard three circles theorem.

Books Recommended:
2. S.Ponnusamy : Foundations of Complex Analysis, Narosa Pub, `97

References:
2. Alfohrs : Complex Analysis

E-references:
1. Introduction to Complex Analysis
2. Complex Analysis
   www.umn.edu/~arnold/502.s97/complex.pdf
M 101
DIFFERENTIAL EQUATIONS-I

Pre-requisites: Chapters 1 to 5 of reference [2]

Unit I:
Initial value problems and the equivalent integral equation, mth order equation in d-dimensions as a first order system, concepts of local existence, existence in the large and uniqueness of solutions with examples. Basic theorems: Ascoli- Arzela theorem, a theorem on convergence of solutions of a family of initial value problems. Picard-Lindel of theorem, Peano's existence theorem and corollary.

Unit II:
Maximal interval of existence, Extension theorem and corollaries, Kamke's convergence theorem, Knesser's theorem. (Statement only) Differential inequalities and uniqueness: Gronwall's inequality, Maximal and minimal solutions, Differential inequalities.

Unit III:
A theorem of Wintner, Uniqueness theorems, Nagumo's and Osgood's criteria. Egres points and Lyapunov functions, Successive approximations.

Unit IV:
Linear differential equations: Linear systems, Variation of constants, reduction to smaller systems, Basic inequalities, constant coefficients.

Unit V:
Floquet theory, adjoint systems, Higher order equations. Dependence on initial conditions and parameters: Preliminaries, continuity, and differentiability.

Books Recommended:

References:

E-references:
1. Ordinary Differential Equations, Modern Perspective Mohan C Joshi IITBombay
   http://www.math.iitb.ac.in/~mcj/root.pdf
2. Differential Equations, Paul Dawkins
3. Ordinary Differential Equations-Lecture Notes, Eugen J. Ionascu
Pre-requisites: Basics on rings and fields.(relevant parts of reference [1])

Unit I:
Modules: Basic definitions, direct products and sums, Free modules.

Unit II:
Noetherian rings and modules, Hilbert Basis Theorem, Power series, Associated primes, primary decomposition.

Unit III:
Modules over PID's, decomposition over one endomorphism, Characteristic polynomial, Jordan & Rational canonical forms.

Unit IV:
Semisimplicity: Matrices & Linear maps over non-commutative rings, conditions defining semisimplicity, the Density theorem,

Unit V:
semisimple rings & simple rings .Representations of finite groups.

Book Recommended:
1. Serge Lang : Algebra

Reference Books:
REAL ANALYSIS-II

Pre-requisites: Algebra of sets, $\sigma$ algebra, Riemann integration

Unit I:
Lebesgue outer measure, measurable sets, a non measurable set

Unit II:
Hausdorff measures on the real line, Hausdorff dimension, Hausdorff dimensions of a Cantor like set.

Unit III:
measurable functions, Littlewoods three principles, a non Borel measurable set, Egoroff’s theorem

Unit IV:
The Lebesgue integral of a bounded function over a set of finite measure, the integral of a nonnegative function, the general Lebesgue integral, properties of these integrals, convergence theorems.

Unit V:
Differentiation of monotone functions, functions of bounded variation, differentiation of an integral, absolute continuity, convex functions, the $L^p$ spaces, the Minkowski and Holder inequalities, convergence and completeness, Bounded linear functionals on $L^p$ spaces.

Books Recommended:


References:

E-references:

2. Review of Lebesgue Measure and Integration, Christopher E. Heil, School of Mathematics Georgia Institute of Technology
   http://people.math.gatech.edu/~heil/handouts/real.pdf
3. Measure Theory and Lebesgue Integration, Joshua H. Lifton
   http://web.media.mit.edu/~lifton/snippets/measure_theory.pdf
4. The Lebesgue Measure and Integral, Mike Klaas
M 213
TOPOLOGY – II

Pre-requisites: M113

Unit I:

Unit II:

Unit III:
First and second countable spaces. Lindelof's theorems. Second countability and separability. Countability and product spaces. Separation axioms. T0, T1, T2, T3, T4; their characterization and basic properties. Urysohn's lemma.

Unit IV:

Unit V:
The fundamental group and covering spaces: Homotopy of paths. The fundamental group. Covering spaces. The fundamental group of the circle and the fundamental theorem of algebra.

Books Recommended:
1. James R. Munkres, Topology (Second edition), Prentice-hall of India

References:

E-references:
1. Topology Course Lecture Notes Aisling McCluskey and Brian McMaster
   http://at.yorku.ca/i/a/a/b/23.htm
2. Notes on Introductory Point-Set Topology, Allen Hatcher
   http://www.math.cornell.edu/~hatcher/Top/TopNotes.pdf
3. Introduction to Topology, Renzo
   http://www.math.colostate.edu/~renzo/teaching/Topology10/Notes.pdf
4. Topology Lecture Notes, Thomas Ward, UEA
   http://www.uea.ac.uk/~h720/teaching/topology/materials/topology.pdf
M 214
COMPLEX ANALYSIS-II

Pre-requisites: Basic Metric space theory: relevant parts of reference [1]

Unit I:
Spaces of analytic functions, Hurwitz's theorem, Montel's theorem, Riemann
Mapping theorem, Weierstrass Factorisation theorem.

Unit II: Gamma function & it's properties, Riemann Zeta function, Riemann's functional
equation, Runge's theorem and Mittag-Leffler's theorem.

Unit III: Analytic continuation, uniqueness of direct analytic continuation and analytic
continuation along a curve, power series method of analytic continuation,
Schwartz Reflection Principle, Monodromy theorem and it's consequences.

Unit IV: Harmonic functions on a disk, Dirichlet problem, Green's function.

Unit V: Canonical products, Jensen's formula, order of an entire function, exponent of
convergence, Hadamard's factorization theorem, range of an analytic function, Bloch's
theorem, The Little Picard theorem, Schottky's theorem, Great Picard theorem.

Books Recommended:
2. S.Ponnusamy : Foundations of Complex Analysis, Narosa Pub, `97

References:
1. Alfohrs : Complex Analysis

E-references:
1. Introduction to Complex Analysis
2. Complex Analysis
   www.umn.edu/~arnold/502.s97/complex.pdf
M 201

DIFFERENTIAL EQUATIONS-II

Pre-requisites: M101

Unit I:
Poincare- Bendixson theory: Autonomous systems, Umlanfsatz, index of a stationary point, Poincare- Bendixson theorem, stability of periodic solutions,

Unit II:
rotation points, foci, nodes and saddle points. Linear second order equations: Preliminaries, Basic facts, Theorems of Sturm,

Unit III:
Sturm-Liouville boundary value problems, Number of zeros,

Unit IV:
Nonoscillatory equations and principal solutions, Nonoscillation theorems.

Unit V:
Use of Implicit function and fixed point theorems: Periodic solutions, linear equations, nonlinear problems.

Books recommended:

References:

E-references:
1. Ordinary Differential Equations, Modern Perspective Mohan C Joshi IITBombay
   http://www.math.iitb.ac.in/~mcj/root.pdf
2. Differential Equations, Paul Dawkins
3. Ordinary Differential Equations-Lecture Notes, Eugen J. Ionascu
SEMESTER – III

M 311

INTEGRATION THEORY

Pre-requisites: Lebesgue Measure theory [1]

Unit I:
Measure spaces, Measurable functions, Integration, Convergence theorems.

Unit II: Signed measures, The Radon-Nikodym theorem, Lebesgue decomposition, \( L^p \) spaces, Riesz representation theorem.
[1] Chapter 11

Unit III: Outer measure and measurability, The extension theorem, Lebesgue-Steiltjes integral, Product measures, Fubini’s theorem.
[1] Chapter 12, Sections 1,2,3,4.

Unit IV: Baire sets, Baire Measure, Continuous functions with compact support, Regularity of measures on locally compact spaces.

Unit V: Integration of continuous functions with compact support, Riesz-Markoff theorem.

Recommended Books:

E-references:
1. Notes on measure and integration in locally compact – Mathematics
   http://math.berkeley.edu/~arveson/Dvi/rieszMarkov.pdf
M 312

FUNCTIONAL ANALYSIS

**Pre-requisites:** Metric spaces, compactness, connectedness.

**Unit I:**
Completion of a metric space, Normed linear spaces. Banach spaces and examples. Quotient space of normed linear space and its completeness.

**Unit II:**
Equivalent norms. Riesz lemma, basic properties of finite dimensional normed linear space and compactness. Weak convergence and bounded.

**Unit III:**
Linear transformations, normed linear spaces of bounded linear transformations, dual spaces with examples. Open mapping and closed graph theorems. Uniform boundedness theorem and some of its consequences, the Hahn-Banach theorem.

**Unit IV:**
Reflexive spaces. Weak sequential compactness.

**Unit V:**

**Recommended Books :**
4. B.V. Limaye, Functional Analysis, New Age Intergration (P) Ltd., 1996

**E-references:**
2. [http://www.math.dauniv.ac.in/Dr.MaheshNDumaldar.php](http://www.math.dauniv.ac.in/Dr.MaheshNDumaldar.php)
PARTIAL DIFFERENTIAL EQUATIONS

Unit I:

Unit II:

Unit III:

[1] Chapter 1 Art. 1.1, 1.2, Chapter. 2

Unit IV:
Nonlinear First Order PDE-Complete Integrals, Envelopes, Characteristics,

Unit V:
Hamilton-Jacobi Equations (Calculus of Variations, Hamilton's ODE, Legendre Transform, Hopf-Lax Formula, Weak Solutions, Uniqueness),

[1] Chapter. 3 Art. 3.1 to 3.3

Recommended Books:

Reference Books:

E-references:
1. PARTIAL DIFFERENTIAL EQUATIONS MA 3132 LECTURE NOTES, B. Neta (http://www.math.nps.navy.mil/~bneta/pde.pdf)
2. Notes for Partial Differential Equations, Kuttler (http://www.math.byu.edu/~klkuttle/547notesB.pdf)
M 301
THEORY OF LINEAR OPERATORS-I

Pre-requisites: Basic linear algebra and basic functional analysis.

Unit I:
Spectral theory of normed linear spaces, resolvent set and spectrum, spectral properties of bounded linear operators, properties of resolvent and spectrum. [1] Chapter 7

Unit II:
spectral mapping theorem for polynomials, spectral radius of bounded linear operator on a complex Banach space, elementary theory of Banach Algebras. [1] Chapter 7

Unit III:
Basic properties of compact linear operators. [1] Chapter 8

Unit IV:
Behaviour of Compact linear operators with respect to solvability of operator equations, Fredholm type theorems, Fredholm alternative theorem, Fredholm alternative for integral equations. [1] Chapter 8

Unit V:
Spectral properties of bounded self-adjoint linear operators on a complex Hilbert space, positive operators, Monotone sequence theorem for bounded self-adjoint operators on a complex Hilbert space, square roots of a positive operator, projection operators. [1] Chapter 9, Sec 9.1-9.6

Recommended Book:

Reference Books:
M 302

Linear Programming - I

**Pre-requisites:** Finite dimensional vector spaces, Linear transformations, Linear system of equations, basic solutions

**Unit I:**
Inverse of matrix by partition, product form of the inverse, basis to basis lemma, lines & hyperplanes, Convex sets and hyperplanes, polyhedral sets, extreme points, faces, directions and extreme directions, Decomposition theorem for polyhedra, Farkas’ lemma.

**Unit II:**
Theory of simplex method, reduction of any feasible solution to a basic feasible solution, improving a basic feasible solution, unbounded solutions, optimality conditions, alternate optima, extreme points and basic feasible solutions,

**Unit III:**
computational aspects of the simplex method, initial basic feasible solution, inconsistency and redundancy, review of the simplex method, Big M method, two phase method

**Unit IV:**
resolution of degeneracy, Charne’s perturbation method, Blande’s rule, Revised simplex method, the simplex method for bounded variables.

**Unit V:**

**Recommended Books:**
Reference Books:
5. Chvatal V., Linear programming, Freeman, NewYork, 1983

E-references:
SEMESTER – IV

M 411
MECHANICS

Unit I:

Unit II:

Unit III:

Unit IV:
Hamilton's principle, Principle of least action.

Unit V:
Books Recommended:


Reference Books:

Pre-requisites: M 301

Unit I:
Spectral family of a bounded self-adjoint linear operator and it's properties, spectral representation of bounded self-adjoint linear operators, spectral theorem
[1] Chapter 9, Sec 9.7-9.11

Unit II:
Unbounded linear operators in Hilbert space, Hellinger-Toeplitz theorem. [1] Chapter 10

Unit III:
Hilbert adjoint operators, Symmetric and self-adjoint linear operators, closed linear operators and closures, spectrum of an unbounded self-adjoint linear operator.
[1] Chapter 10

Unit IV:
spectral theorem for unitary and self adjoint linear operators. [1] Chapter 10

Unit V:
Multiplication operator and Differentiation operator. [1] Chapter 10

Recommended Book:

Reference Book:
Pre-requisites: M401

Unit I:
Duality theory, weak and strong duality theorems, Complementary slackness, dual simplex method, primal dual algorithm, Integer programming, the KKT conditions.

Unit II:
Transportation problems, properties of the activity matrix of a transportation problem, simplification of the simplex method to the transportation problem, bases in a transportation problem, the stepping stone algorithm, resolution of degeneracy, determination of an initial basic feasible solution, alternative procedure for computing $z_{ij} - c_{ij}$ using duality(u-v method).

Unit III:
Assignment problems, reduced cost coefficient matrix, the Hungarian method, Konig – Eевgany theorem, The Birkoff –von Neumann theorem.

Unit IV:
Sensitivity analysis, the Dantzig-Wolf decomposition, Game theory and linear programming, Two person zero sum games, Games with mixed strategies, Graphical solution, Solution by linear programming.

Unit V:
Applications: Optimal product mix and activity levels, Petroleum refinery operations, Blending problems, Economic interpretation of dual linear programming problems, Input output analysis, Leotief systems.
**Recommended Books:**


**Reference Books:**

5. Chvatal V., Linear programming, Freeman, New York, 1983

**E-references:**

1. [http://www.math.dauniv.ac.in/Dr.MaheshNDumaldar.php](http://www.math.dauniv.ac.in/Dr.MaheshNDumaldar.php)
3. National Programme on Technology Enhanced Learning (Mathematics)
M 403
HOMOTOPY THEORY

Pre-requisites: M113 & M213

Unit I:
The Fundamental Group, Homotopic Paths and the Fundamental Group.

Unit II:
The Covering Homotopy Property for $S^1$, Examples of Fundamental Groups.

Unit III:

Unit IV:
The Higher Homotopy Groups, Equivalent Definitions of $\pi_n(X, x_0)$, Basic Properties and Examples.

Unit V:

Recommended Book:
TOPICS IN RING THEORY

Pre-requisites: Basic definitions and results concerning rings and fields.

Unit I:
Rings and Ring Homomorphisms, Ideals Quotient Rings, Zero Divisors, Nilpotent Elements, Units.

Unit II:

Unit III:
Modules, Operation on Submodules, Direct Sum and Product of Modules, Restriction and Extension of Scalars.

Unit IV:
Tensor product of modules, basic properties, Exactness Properties of Tensor Product, Algebras & Tensor Product of Algebras.

Unit V:
Rings and Modules of Fractions, Local Properties Extended and Contracted Ideals in Ring of Fractions. (with Emphasis an Exercise) [1 chapter 1 to 3]

Books Recommended:

E-references:
1. Commutative Algebra Notes Branden Stone
   math.bard.edu/~bstone/commalg-notes/
2. Commutative Algebra Lecture Notes - Tata Institute of Fundamental
   www.math.tifr.res.in/~anands/CA-Lecture%20notes.pdf
M 405

ALGEBRAIC TOPOLOGY

Pre-requisites: M113 & M213

UNIT I :
Deformation retracts and homotopy type. Fundamental group of \( S^n \) for \( n > 1 \), and some surfaces. The Jordan separation theorem, the Jordan curve theorem, Imbedding graphs in plane.
[1] Chapter 9, sections 58 to 60 & Chapter 10, sections 61, 63 and 64.

UNIT II :
[1] Chapter 11, sections 68 to 73 & Chapter 12, sections 74 to 78.

Unit III :

UNIT IV :
[2] Chapter 3, Sections 23 to 28 (relevant portions)
UNIT V:


[2] Chapter 5, Sections 41 to 49.

Books recommended:

Unit I: Characters of finite abelian groups, The character group, Dirichlet characters, Sums involving Dirichlet characters, Dirichlet's theorem on primes in arithmetic progressions. [1] Chapter 6, sections 6.5 to 6.10, Chapter 7

Unit II: Dirichlet series and Euler products, the function defined by Dirichlet series, The half-plane of convergence of a Dirichlet series, Integral formula for the coefficients of Dirichlet series, etc. [1] Chapter 11

Unit III: Properties of the gamma functions, Integral representations of Hurwitz zeta functions, Analytic continuation of Hurwitz zeta functions, Functional equation for the Riemann zeta function and properties of Riemann zeta functions etc. [1] Chapter 12

Unit IV: Analytic proof of prime number theorem. [1] Chapter 13

Unit V: Geometric representation of partitions, Generating functions of partitions, Euler's pentagonal number theorem, Euler's recursion formula for $p(n)$, Jacobi's triple product identity, The partition identity of Ramanujan. [1] Chapter 14

Book Recommended:
Unit I : Definition of a topological group and its basic properties. Subgroups and quotient groups. Product groups & projective limits. [1], Sections 4,5,6 of Chapter Two.

Unit II : Properties of topological groups involving connectedness. Invariant pseudo-metrics and separation axioms. Structure theory for compact and locally compact Abelian groups. Some special locally compact Abelian groups. [1], Sections 7,8,9,10 of Chapter Two.

Unit III : The Haar integral. Haar Measure. Invariant means defined for all bounded functions. Invariant means of almost periodic functions. [1], Chapter Four.

Unit IV : Convolutions, Convolutions of functions and measures. Elements of representation theory. Unitary representations of locally compact groups. [1], Chapter Five.

Unit V : The character group of a locally compact Abelian group and the duality theorem. [1], Sections 23,24 of Chapter Six.

Recommended Book :

Reference :